



BioTriangle

--BioDNA features



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1. Nucleic acid composition

The most straight forward approach to represent the DNA sequences is based on their nucleic acid composition. The kmer and its variants have been widely used for this aim. Here, BioDNA allows users to calculate various kinds of kmer-based feature vectors for given sequences or FASTA files by selecting different methods and parameters. This module aims at computing three types of nucleic acid composition, including basic kmer, reverse compliment kmer and increment of diversity. Let's introduce them one by one.

1.1 Basic kmer

Basic kmer is the simplest approach to represent the DNAs, in which the DNA sequences are represented as the occurrence frequencies of k neighboring nucleic acids. This approach has been successfully applied to human gene regulatory sequence prediction (Noble, et al., 2005), enhancer identification (Lee, et al., 2011), etc.

The parameters:

- k : the k value of kmer, it should be an integer larger than 0.
- *normalize*: with this option, the final feature vector will be normalized based on the total occurrences of all kmers. Therefore, the elements in the feature vectors represent the frequencies of kmers. The default value of this parameter is **True**.

1.2 Reverse compliment kmer

The reverse compliment kmer is a variant of the basic kmer, in which the kmers are not expected to be strand-specific, so reverse complements are collapsed into a single feature. For example, if $k=2$, there are totally 16 basic kmers ('AA', 'AC', 'AG', 'AT', 'CA', 'CC', 'CG', 'CT', 'GA', 'GC', 'GG', 'GT', 'TA', 'TC', 'TG', 'TT'), but by removing the reverse compliment kmers, there are only 10 distinct kmers in the reverse compliment kmer approach ('AA', 'AC', 'AG', 'AT', 'CA', 'CC', 'CG', 'GA', 'GC', 'TA'). For more information of this approach, please refer to (Noble, et al., 2005) (Gupta, et al., 2008)

The parameters:

- k : the k value of kmer, it should be an integer larger than 0.
- *normalize*: with this option, the final feature vector will be normalized based on the total occurrences of all kmers. Therefore, the elements in the feature vector represent the frequencies of kmers. The default value of this parameter is **True**.

1.3 Increment of diversity

The increment of diversity has been successfully applied in the prediction of exon-intron splice sites for several model genomes (Zhang and Luo, 2003), transcription start site prediction, and studying the organization of nucleosomes around splice sites(Lv and Luo, 2008).

In this method, the sequence features are converted into the increment of diversity (ID), defined by the relation of sequence X with standard source S :

$$ID = \text{Diversity}(X+S) - \text{Diversity}(S) - \text{Diversity}(X) \quad (2)$$

Given a sequence X with r feature variables (ID_1 to ID_r), we obtain an r -dimensional feature vector $\mathbf{R} = (ID_1, ID_2, \dots, ID_r)$. The feature vector \mathbf{R} is designed by the following considerations. The kmers are responsible for the discrimination between positive samples and negative samples, and therefore they construct the diversity sources. Based on this, 2 kmer-based increments of diversities ID_1 (ID_2) between sequence X and the standard source in positive (negative) training set can be easily introduced as the feature vectors.

For more information of this approach, please refer to (Chen, et al., 2010) and (Liu, et al., 2012).

The parameters:

- k : the k value of kmer, it should be an integer larger than 0, the default value is 6.

Note: This feature is temporally not included in BioDNA (Version 1.0).

2. Autocorrelation

Autocorrelation, as one of the multivariate modeling tools, can transform the DNA sequences of different lengths into fixed-length vectors by measuring the correlation between any two properties. Autocorrelation results in two kinds of variables: autocorrelation (AC) between the same property, and cross-covariance (CC) between

two different properties. Here, BioDNA allows users to calculate various kinds of autocorrelation feature vectors for given DNA sequences or FASTA files by selecting different methods and parameters. This module aims at computing six types of autocorrelation, including dinucleotide-based auto covariance (DAC), dinucleotide-based cross covariance (DCC), dinucleotide-based auto-cross covariance (DACC), trinucleotide-based auto covariance (TAC), trinucleotide-based cross covariance (TCC), and trinucleotide-based auto-cross covariance (TACC). Let's introduce them one by one.

2.1 Dinucleotide-based auto covariance

Suppose a DNA sequence D with L nucleic acid residues; i.e.

$$\mathbf{D} = R_1 R_2 R_3 R_4 R_5 R_6 R_7 \cdots R_L \quad (3)$$

where R_1 represents the nucleic acid residue at the sequence position 1, R_2 the nucleic acid residue at position 2 and so forth.

The DAC measures the correlation of the same physicochemical index between two dinucleotide separated by a distance of lag along the sequence, which can be calculated as:

$$DAC(u, lag) = \sum_{i=1}^{L-lag-1} (P_u(R_i R_{i+1}) - \bar{P}_u)(P_u(R_{i+lag} R_{i+lag+1}) - \bar{P}_u) / (L-lag-1) \quad (4)$$

where u is a physicochemical index, L is the length of the DNA sequence, $P_u(R_i * R_{i+1})$ means the numerical value of the physicochemical index u for the dinucleotide $R_i * R_{i+1}$ at position i , \bar{P}_u is the average value for physicochemical index u along the whole sequence:

$$\bar{P}_u = \sum_{j=1}^{L-1} P_u(R_j R_{j+1}) / (L-1) \quad (5)$$

In such a way, the length of DAC feature vector is $N*LAG$, where N is the number of physicochemical indices and LAG is the maximum of lag ($lag = 1, 2, \dots, LAG$).

This DAC approach is similar as the approach used for protein fold recognition (Dong, et al., 2009).

The parameters:

- *lag*: an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the length of the shortest DNA sequence in the dataset). It represents the distance between two dinucleotides.
- *phyche_index*: the physicochemical indices, it should be a list type and there are 38 different physicochemical indices (**Table 1**), which the users can choose.

2.2 Dinucleotide-based cross covariance

Given a DNA sequence D (Eq. 3), the DCC approach measures the correlation of two different physicochemical indices between two dinucleotides separated by lag nucleic acids along the sequence, which can be calculated by:

$$DCC(u_1, u_2, lag) = \sum_{i=1}^{L-lag-1} (P_{u_1}(R_i R_{i+1}) - \bar{P}_{u_1})(P_{u_2}(R_{i+lag} R_{i+lag+1}) - \bar{P}_{u_2}) / (L - lag - 1) \quad (6)$$

where u_1, u_2 are two different physicochemical indices, L is the length of the DNA sequence, $P_{u_1}(R_i R_{i+1})$ ($P_{u_2}(R_i R_{i+1})$) is the numerical value of the physicochemical

index u_1 (u_2) for the dinucleotide $R_i * R_{i+1}$ at position i , \bar{P}_{u_1} (\bar{P}_{u_2}) is the average value for physicochemical index value u_1, u_2 along the whole sequence:

$$\bar{P}_u = \sum_{j=1}^{L-1} P_u(R_j R_{j+1}) / (L-1) \quad (7)$$

In such a way, the length of the DCC feature vector is $N*(N-1)*LAG$, where N is the number of physicochemical indices and LAG is the maximum of lag ($lag=1, 2, \dots, LAG$).

This DCC approach is similar as the approach used for protein fold recognition (Dong, et al., 2009).

The parameters:

- *lag*: an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the length of the shortest DNA sequence in the dataset). It represents the distance between two dinucleotides.
- *phyche_index*: the physicochemical indices, it should be a list type and there are 38 different physicochemical indices (Table 1), which the users can choose.

2.3 Dinucleotide-based auto-cross covariance

DACC is a combination of DAC and DCC. Therefore, the length of the DACC feature vector is $N*N*LAG$, where N is the number of physicochemical indices and LAG is the maximum of lag ($lag = 1, 2, \dots, LAG$).

The parameters:

- *lag*: an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the

length of the shortest DNA sequence in the dataset). It represents the distance between two dinucleotides.

- *phyche_index*: the physicochemical indices, it should be a list type and there are 38 different physicochemical indices (**Table 1**), which the users can choose.

2.4 Trinucleotide-based auto covariance

Given a DNA sequence D (**Eq. 3**), the TAC approach measures the correlation of the same physicochemical index between two trinucleotides separated by *lag* nucleic acids along the sequence, which can be calculated as:

$$TAC(lag, u) = \sum_{i=1}^{L-lag-2} (P_u(R_i R_{i+1} R_{i+2}) - \bar{P}_u)(P_u(R_{i+lag} R_{i+lag+1} R_{i+lag+2}) - \bar{P}_u) / (L-lag-2) \quad (8)$$

where *u* is a physicochemical index, *L* is the length of the DNA sequence,

$P_u(R_i R_{i+1} R_{i+2})$ represents the numerical value of the physicochemical index *u* for the trinucleotide $R_i R_{i+1} R_{i+2}$ at position *i*, \bar{P}_u is the average value for physicochemical index *u* value along the whole sequence:

$$\bar{P}_u = \sum_{j=1}^{L-2} P_u(R_j R_{j+1} R_{j+2}) / (L-2) \quad (9)$$

In such a way, the length of TAC feature vector is $N*LAG$, where *N* is the number of physicochemical indices and *LAG* is the maximum of *lag* ($lag=1, 2, \dots, LAG$).

The parameters:

- *lag*: an integer larger than or equal to 0 and less than or equal to $L-3$ (*L* means the length of the shortest DNA sequence in the dataset). It represents the distance between two trinucleotides.
- *phyche_index*: the physicochemical indices, it should be a list and there are 12 different physicochemical indices (**Table 2**), which the users can choose.

2.5 Trinucleotide-based cross covariance

Given a DNA sequence D (**Eq. 3**), the TCC approach measures the correlation of two different physicochemical indices between two trinucleotides separated by *lag* nucleic acids along the sequence, which can be calculated by:

$$\text{TCC}(u_1, u_2, \text{lag}) = \sum_{i=1}^{L-\text{lag}-2} (P_{u_1}(R_i R_{i+1} R_{i+2}) - \bar{P}_{u_1})(P_{u_2}(R_{i+\text{lag}} R_{i+\text{lag}+1} R_{i+\text{lag}+2}) - \bar{P}_{u_2}) / (L-\text{lag}-2) \quad (10)$$

where u_1, u_2 are two physicochemical indices, L is the length of the DNA sequence, $P_{u_1}(R_i R_{i+1} R_{i+2})$ ($P_{u_2}(R_i R_{i+1} R_{i+2})$) represents the numerical value of the physicochemical index u_1 (u_2) for the trinucleotide $R_i R_{i+1} R_{i+2}$ at position i , \bar{P}_{u_1} (\bar{P}_{u_2}) is the average value for physicochemical index value u_1 (u_2) along the whole sequence:

$$\bar{P}_u = \sum_{j=1}^{L-2} P_u(R_j R_{j+1} R_{j+2}) / (L-2) \quad (11)$$

In such a way, the length of TCC feature vector is $N*(N-1)*\text{LAG}$, where N is the number of physicochemical index and LAG is the maximum of lag ($\text{lag} = 1, 2, \dots, \text{LAG}$).

The parameters:

- *lag*: an integer larger than or equal to 0 and less than or equal to $L-3$ (L means the length of the shortest sequence in the dataset). It represents the distance between two trinucleotides.
- *Phyche_index*: the physicochemical indices, it should be a list and there are 12 different physicochemical indices (**Table 2**), which the users can choose.

2.6 Trinucleotide-based auto-cross covariance

TACC is a combination of TAC and TCC. Therefore, the length of the TACC feature vector is $N*N*\text{LAG}$, where N is the number of physicochemical indices and LAG is the maximum of lag ($\text{lag} = 1, 2, \dots, \text{LAG}$).

The parameters:

- *lag*: an integer larger than or equal to 0 and less than or equal to $L-3$ (L means the length of the shortest DNA sequence in the dataset). It represents the distance between two trinucleotides.
- *phyche_index*: the physicochemical indices, it should be a list and there are 12 different physicochemical indices (**Table 2**), which the users can choose.

3. Pseudo nucleic acid composition

PseNAC is a kind of powerful approaches to represent the DNA sequences considering both DNA local sequence-order information and long range or global sequence-order effects. Here, BioDNA allows users to calculate various kinds of PseNAC based feature vectors for given sequences or FASTA files by selecting different methods and parameters. This module aims at computing six types of pseudo nucleic acid composition: pseudo dinucleotide composition (PseDNC), pseudo k-tuple nucleotide composition (PseKNC), parallel correlation pseudo dinucleotide composition (PC-PseDNC), parallel correlation pseudo trinucleotide composition (PC-PseTNC), series correlation pseudo dinucleotide composition (SC-PseDNC), and series correlation pseudo trinucleotide composition (SC-PseTNC). Let's introduce them one by one.

3.1 Pseudo dinucleotide composition

PseDNC is an approach incorporating the contiguous local sequence-order information and the global sequence-order information into the feature vector of the DNA sequence.

Given a DNA sequence D (Eq. 3), the feature vector of D is defined:

$$\mathbf{D} = [d_1 \ d_2 \ \cdots \ d_{16} \ d_{16+1} \ \cdots \ d_{16+\lambda}]^T \quad (12)$$

where

$$d_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{16} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (1 \leq k \leq 16) \\ \frac{w\theta_{k-16}}{\sum_{i=1}^{16} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (17 \leq k \leq 16 + \lambda) \end{cases} \quad (13)$$

where $f_k (k=1,2,\dots,16)$ is the normalized occurrence frequency of dinucleotide in the DNA sequence; the parameter λ is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; w is the weight factor ranged from 0 to 1; $\theta_j (j=1,2,\dots,\lambda)$ is called the j -tier correlation factor that reflects the sequenceorder correlation between all the most contiguous dinucleotide along a DNA sequence, which is defined:

$$\left\{ \begin{array}{l} \theta_1 = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_i R_{i+1}, R_{i+1} R_{i+2}) \\ \theta_2 = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_i R_{i+1}, R_{i+2} R_{i+3}) \\ \theta_3 = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_i R_{i+1}, R_{i+3} R_{i+4}) \\ \dots\dots \\ \theta_\lambda = \frac{1}{L-1-\lambda} \sum_{i=1}^{L-1-\lambda} \Theta(R_i R_{i+1}, R_{i+\lambda} R_{i+\lambda+1}) \end{array} \right. \quad (\lambda < L) \quad (14)$$

$$\left\{ \begin{array}{l} \theta_1 = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_i R_{i+1}, R_{i+1} R_{i+2}) \\ \theta_2 = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_i R_{i+1}, R_{i+2} R_{i+3}) \\ \theta_3 = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_i R_{i+1}, R_{i+3} R_{i+4}) \\ \dots\dots \\ \theta_\lambda = \frac{1}{L-1-\lambda} \sum_{i=1}^{L-1-\lambda} \Theta(R_i R_{i+1}, R_{i+\lambda} R_{i+\lambda+1}) \end{array} \right. \quad (\lambda < L) \quad (14)$$

where the correlation function is given by

$$\Theta(R_i R_{i+1}, R_j R_{j+1}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1}) - P_u(R_j R_{j+1})]^2 \quad (15)$$

where μ is the number of physicochemical indices, in this study, 6 indices reflecting the local DNA structural properties (Table 3) were employed to generate the PseDNC feature vector; $P_u(R_i R_{i+1})$ represents the numerical value of the u -th ($u = 1, 2, \dots, \mu$)

physicochemical index of the dinucleotide $R_i R_{i+1}$ at position i and $P_u(R_j R_{j+1})$ represents the corresponding value of the dinucleotide $R_j R_{j+1}$ at position j . For more information about this approach, please refer to (Chen, et al., 2013).

The parameters:

- *lamada*: an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the length of the shortest sequence in the dataset). It represents the highest counted rank (or tier) of the correlation along a DNA sequence. Its default value is 3.
- w : the weight factor ranged from 0 to 1. Its default value is 0.05.

3.2 Pseudo k -tupler composition

PseKNC improved the PseDNC approach by incorporating k -tuple nucleotide

composition.

Given a DNA sequence D (Eq. 3), the feature vector of D is defined:

$$\mathbf{D} = [d_1 \ d_2 \ \cdots \ d_{4^k} \ d_{4^k+1} \ \cdots \ d_{4^k+\lambda}]^T \quad (16)$$

where

$$d_u = \begin{cases} \frac{f_u}{\sum_{i=1}^{4^k} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (1 \leq u \leq 4^k) \\ \frac{w \theta_{u-4^k}}{\sum_{i=1}^{4^k} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (4^k \leq u \leq 4^k + \lambda) \end{cases} \quad (17)$$

where λ is the number of the total counted ranks (or tiers) of the correlations along a DNA sequence; f_u ($u=1,2,\dots,4^k$) is the frequency of oligonucleotide that is normalized to $\sum_{i=1}^{4^k} f_i = 1$; w is a weight factor; θ_j is given by

$$\theta_j = \frac{1}{L-j-1} \sum_{i=1}^{L-j-1} \Theta(R_i R_{i+1}, R_{i+j} R_{i+j+1}) \quad (j=1, 2, \dots, \lambda; \lambda < L) \quad (18)$$

which represents the j -tier structural correlation factor between all the j^{th} most contiguous dinucleotides. The correlation function $\Theta(R_i R_{i+1}, R_{i+j} R_{i+j+1})$ is defined by

$$\Theta(R_i R_{i+1}, R_{i+j} R_{i+j+1}) = \frac{1}{\mu} \sum_{v=1}^{\mu} [P_v(R_i R_{i+1}) - P_v(R_{i+j} R_{i+j+1})]^2 \quad (19)$$

where μ is the number of physicochemical indices, in this study, 6 indices reflecting the local DNA structural properties (Table 3) were employed to generate the PseKNC feature vector; $P_v(R_i R_{i+1})$ represents the numerical value of the v -th ($v = 1, 2, \dots, \mu$)

physicochemical indices for the dinucleotide $R_i R_{i+1}$ at position i and $P_v(R_{i+j} R_{i+j+1})$

represents the corresponding value for the dinucleotide $R_{i+j} R_{i+j+1}$ at position $i+j$.

For more information about this approach, please refer to (Guo, et al., 2014)

The parameters:

- k : an integer larger than 0 represents the k -tuple. Its default value is 3.
- λ : an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the length of the shortest DNA sequence in the dataset), representing the highest counted rank (or tier) of the correlation along a DNA sequence. The default value is 1.
- w : the weight factor ranged from 0 to 1. Its default value is 0.05.

3.3 Parallel correlation pseudo dinucleotide composition

In PC-PseDNC approach, the users cannot only select the 38 built-in physicochemical

indices (**Table 1**), but also can upload their own indices to generate the PC-PseDNC feature vector.

Given a DNA sequence D (**Eq. 3**), the PC-PseDNC feature vector of D is defined:

$$\mathbf{D} = [d_1 \ d_2 \ \cdots \ d_{16} \ d_{16+1} \ \cdots \ d_{16+\lambda}]^T \quad (20)$$

where

$$d_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{16} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (1 \leq k \leq 16) \\ \frac{w \theta_{k-16}}{\sum_{i=1}^{16} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (17 \leq k \leq 16 + \lambda) \end{cases} \quad (21)$$

where f_k ($k=1,2,\dots,16$) is the normalized occurrence frequency of dinucleotide in the DNA sequence; the parameter λ is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; w is the weight factor ranged from 0 to 1; θ_j ($j=1, 2, \dots, \lambda$) is called the j -tier correlation factor that reflects the sequence order correlation between all the most contiguous dinucleotides along a DNA sequence, which is defined:

$$\begin{cases} \theta_1 = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_i R_{i+1}, R_{i+1} R_{i+2}) \\ \theta_2 = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_i R_{i+1}, R_{i+2} R_{i+3}) \\ \theta_3 = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_i R_{i+1}, R_{i+3} R_{i+4}) \\ \dots \\ \theta_\lambda = \frac{1}{L-1-\lambda} \sum_{i=1}^{L-1-\lambda} \Theta(R_i R_{i+1}, R_{i+\lambda} R_{i+\lambda+1}) \end{cases} \quad (\lambda < L) \quad (22)$$

where the correlation function is given by

$$\Theta(R_i R_{i+1}, R_j R_{j+1}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1}) - P_u(R_j R_{j+1})]^2 \quad (23)$$

where μ is the number of physicochemical indices considered that are listed in the **Table 1**; $P_u(R_i R_{i+1})$ ($P_u(R_j R_{j+1})$) represents the numerical value of the u -th ($u = 1, 2, \dots, \mu$) physicochemical index for the dinucleotide $R_i R_{i+1}$ ($R_j R_{j+1}$) at position i and j , respectively.

For more information of PC-PseDNC approach, you can refer to (Chen, et al., 2014).

The parameters:

- *lamada*: an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the length of the shortest DNA sequence in the dataset), representing the highest counted rank (or tier) of the correlation along a DNA sequence. Its default value is 1.
- w : the weight factor ranged from 0 to 1, its default value is 0.05.

- *phyche_index*: The 38 built-in physicochemical indices (**Table 1**), which the users can choose. Its type should be a list.

3.4 Parallel correlation pseudo trinucleotide composition

In PC-PseTNC approach, 12 built-in trinucleotide physicochemical indices (**Table 2**) are incorporated to generate the representations of DNA sequences. Furthermore, the user defined indices can be also used to generate the feature vector.

Given a DNA sequence D (**Eq. 3**), the PC-PseTNC feature vector of D is defined:

$$\mathbf{D} = [d_1 \ d_2 \ \cdots \ d_{64} \ d_{64+1} \ \cdots \ d_{64+\lambda}]^T \quad (24)$$

where

$$d_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{64} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (1 \leq k \leq 64) \\ \frac{w \theta_{k-64}}{\sum_{i=1}^{64} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (65 \leq k \leq 64 + \lambda) \end{cases} \quad (25)$$

where f_k ($k=1,2,\dots,64$) is the normalized occurrence frequency of trinucleotide in the DNA sequence; the parameter λ is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; w is the weight factor ranged from 0 to 1; θ_j ($j=1,2,\dots,\lambda$) is called the j -tier correlation factor that reflects the sequence order correlation between all the most contiguous trinucleotide along a DNA sequence, which is defined:

$$\left\{ \begin{array}{l} \theta_1 = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_i R_{i+1} R_{i+2}, R_{i+1} R_{i+2} R_{i+3}) \\ \theta_2 = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_i R_{i+1} R_{i+2}, R_{i+2} R_{i+3} R_{i+4}) \\ \theta_3 = \frac{1}{L-5} \sum_{i=1}^{L-5} \Theta(R_i R_{i+1} R_{i+2}, R_{i+3} R_{i+4} R_{i+5}) \\ \dots \\ \theta_\lambda = \frac{1}{L-2-\lambda} \sum_{i=1}^{L-2-\lambda} \Theta(R_i R_{i+1} R_{i+2}, R_{i+\lambda} R_{i+\lambda+1} R_{i+\lambda+2}) \end{array} \right. \quad (\lambda < L) \quad (26)$$

where the correlation function is given by

$$\Theta(R_i R_{i+1} R_{i+2}, R_j R_{j+1} R_{j+2}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1} R_{i+2}) - P_u(R_j R_{j+1} R_{j+2})]^2 \quad (27)$$

where μ is the number of physicochemical indices (**Table 2**); $P_u(R_i R_{i+1} R_{i+2})$

$(P_u(R_j R_{j+1} R_{j+2}))$ represents the numerical value of the u -th ($u = 1, 2, \dots, \mu$)

physiochemical index for the trinucleotide $R_i R_{i+1} R_{i+2} (R_j R_{j+1} R_{j+2})$ at position $i(j)$.

For more information of PC-PseTNC approach, you can refer to (Chen, et al., 2014) (Qiu, et al., 2014)

The parameters:

- *lamada*: an integer larger than or equal to 0 and less than or equal to $L-3$ (L means the length of the shortest sequence in the dataset), representing the highest counted rank (or tier) of the correlation along a DNA sequence. The default value is 1.
- w : the weight factor ranged from 0 to 1, its default value is 0.05.
- *phyche_index*: the 12 built-in physicochemical indices (**Table 2**), which the users can choose. Its type should be a list.

3.5 Series correlation pseudo dinucleotide composition

SC-PseDNC is a variant of PC-PseDNC. Given a DNA sequence D (Eq. 3), the SCPseDNC feature vector of D is defined:

$$\mathbf{D} = [d_1 \ d_2 \ \cdots \ d_{16} \ d_{16+1} \ \cdots \ d_{16+\lambda} \ d_{16+\lambda+1} \ \cdots \ d_{16+\lambda\Lambda}]^T \quad (28)$$

where

$$d_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{16} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (1 \leq k \leq 16) \\ \frac{w \theta_{k-16}}{\sum_{i=1}^{16} f_i + w \sum_{j=1}^{\lambda\Lambda} \theta_j} & (17 \leq k \leq 16 + \lambda\Lambda) \end{cases} \quad (29)$$

where f_k ($k=1, 2, \dots, 16$) is the normalized occurrence frequency of dinucleotide in the DNA sequence; the parameter λ is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; w is the weight factor ranged from 0 to 1; Λ is the number of physicochemical indices; θ_j ($j = 1, 2, \dots, \lambda$) is called the j -tier correlation factor that reflects the sequence-order correlation between all the most contiguous dinucleotides along a DNA sequence, which is defined:

$$\left\{ \begin{array}{l} \theta_1 = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^1 \\ \theta_2 = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^2 \\ \dots \\ \theta_\Lambda = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^\Lambda \quad \lambda < (L-2) \\ \dots \\ \theta_{\lambda\Lambda-1} = \frac{1}{L-\lambda-2} \sum_{i=1}^{L-\lambda-2} J_{i,i+\lambda}^{\Lambda-1} \\ \theta_{\lambda\Lambda} = \frac{1}{L-\lambda-2} \sum_{i=1}^{L-\lambda-2} J_{i,i+\lambda}^\Lambda \end{array} \right. \quad (30)$$

The correlation function is given by

$$\left\{ \begin{array}{l} J_{i,i+m}^\zeta = P_u(R_i R_{i+1}) \cdot P_u(R_{i+m} R_{i+m+1}) \\ \zeta = 1, 2, \dots, \Lambda; m = 1, 2, \dots, \lambda; i = 1, 2, \dots, L-\lambda-2 \end{array} \right. \quad (31)$$

where μ is the number of total physicochemical indices (**Table 1**); $P_u(R_i R_{i+1})$

$(P_u(R_j R_{j+1}))$ represents the numerical value of the u -th ($u = 1, 2, \dots, \mu$) physicochemical index for the dinucleotide $R_i R_{i+1}$ ($R_j R_{j+1}$) at position $i(j)$.

For more information of the SC-PseDNC, please refer to (Chen, et al., 2014).

The parameters:

- *lamada*: an integer larger than or equal to 0 and less than or equal to $L-2$ (L means the length of the shortest DNA sequence in the dataset), representing the highest counted rank (or tier) of the correlation along a DNA sequence. The default value is 1.
- *w*: the weight factor ranged from 0 to 1, the default value is 0.05.
- *phyche_index*: The 38 built-in physicochemical indices (**Table 1**), which the users can choose. Its type should be a list.

3.6 Series correlation pseudo trinucleotide composition

SC-PseTNC is a variant of PC-PseTNC. Given a DNA sequence D (Eq. 3), the SCPseTNC feature vector of D is defined:

$$\mathbf{D} = [d_1 \ d_2 \ \cdots \ d_{64} \ d_{64+1} \ \cdots \ d_{64+\lambda} \ d_{64+\lambda+1} \ \cdots \ d_{64+\lambda\Lambda}]^T \quad (32)$$

where

$$d_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{64} f_i + w \sum_{j=1}^{\lambda} \theta_j} & (1 \leq k \leq 64) \\ \frac{w\theta_{k-64}}{\sum_{i=1}^{64} f_i + w \sum_{j=1}^{\lambda\Lambda} \theta_j} & (65 \leq k \leq 64 + \lambda\Lambda) \end{cases} \quad (33)$$

where f_k ($k=1, 2, \dots, 64$) is the normalized occurrence frequency of trinucleotide in the DNA sequence; the parameter λ is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; w is the weight factor ranged from 0 to 1; Λ is the number of physicochemical indices; θ_j ($j=1, 2, \dots, \lambda$) is called the j -tier correlation factor that reflects the sequence order correlation between all the most contiguous trinucleotides along a DNA sequence, which is defined:

$$\left\{ \begin{array}{l} \theta_1 = \frac{1}{L-4} \sum_{i=1}^{L-4} J_{i,i+1}^1 \\ \theta_2 = \frac{1}{L-4} \sum_{i=1}^{L-4} J_{i,i+1}^2 \\ \dots\dots \\ \theta_{\lambda} = \frac{1}{L-4} \sum_{i=1}^{L-4} J_{i,i+1}^{\lambda} \quad \lambda < (L-3) \\ \dots\dots \\ \theta_{\lambda\Lambda-1} = \frac{1}{L-\lambda-3} \sum_{i=1}^{L-\lambda-3} J_{i,i+\lambda}^{\Lambda-1} \\ \theta_{\lambda\Lambda} = \frac{1}{L-\lambda-3} \sum_{i=1}^{L-\lambda-3} J_{i,i+\lambda}^{\Lambda} \end{array} \right. \quad (34)$$

The correlation function is given by

$$\left\{ \begin{array}{l} J_{i,i+m}^{\zeta} = P_u(R_i R_{i+1} R_{i+2}) \cdot P_u(R_{i+m} R_{i+m+1} R_{i+m+2}) \\ \zeta = 1, 2, \dots, \Lambda; \ m = 1, 2, \dots, \lambda; \ i = 1, 2, \dots, L-\lambda-3 \end{array} \right. \quad (35)$$

where μ is the number of physicochemical indices (Table 2); $P_u(R_i R_{i+1} R_{i+2})$ ($P_u(R_j R_{j+1} R_{j+2})$) represents the numerical value of the u -th ($u = 1, 2, \dots, \mu$) physicochemical index for the trinucleotide $R_i R_{i+1} R_{i+2}$ ($R_j R_{j+1} R_{j+2}$) at position $i(j)$.

For more information of the SC-PseTNC approach, please refer to (Chen, et al., 2014)

The parameters:

- *lamada*: an integer larger than or equal to 0 and less than or equal to $L-3$ (L means the length of the shortest DNA sequence in the dataset), representing the highest counted rank (or tier) of the correlation along a DNA sequence. The default value is 1.

- w : the weight factor ranged from 0 to 1, the default value is 0.05.
- *pyche_index*: the 12 built-in physicochemical indices (Table 2), which the users can choose. Its type should be a list.

4. Table 1

Base stacking	Protein induced deformability	B-DNA twist
A-philicity	Propeller twist	Duplex stability: (freeenergy)
DNA denaturation	Bending stiffness	Protein DNA twist
Aida_BA_transition	Breslauer_dG	Breslauer_dH
Electron_interaction	Hartman_trans_free_energy	Helix-Coil_transition
Lisser_BZ_transition	Polar_interaction	SantaLucia_dG
SantaLucia_dS	Sarai_flexibility	Stability
Sugimoto_dG	Sugimoto_dH	Sugimoto_dS
Duplex tability (disruptenergy)	Stabilising energy of Z-DNA	Breslauer_dS
Ivanov_BA_transition	SantaLucia_dH	Stacking_energy
Watson-Crick_interaction	Dinucleotide GC Content	Twist
Tilt	Roll	Shift
Slide	Rise	

Note: By now, 37 kinds of *pyche_index* in table 1 is available except “Duplex stability: (freeenergy)”.

5. Table 2

Bendability (DNase)	Bendability (consensus)	Trinucleotide GC Content
Consensus_roll	Consensus-Rigid	Dnase I
MW-Daltons	MW-kg	Nucleosome
Nucleosome positioning	Dnase I-Rigid	Nucleosome-Rigid

6. Table 3

Twist	Tilt	Roll
Shift	Slide	Rise

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